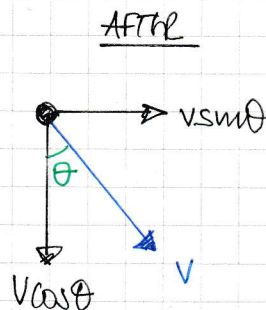
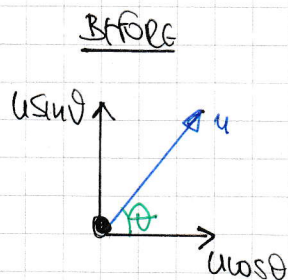


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YGB - FM | PAGE 9 - QUESTION 1

a) STARTING WITH A BEFORE & AFTER DIAGRAM - LET THE "BOUNCING SPEED" BE V



NO MOMENTUM EXCHANGE IN A DIRECTION PARALLEL TO THE WALL

$$\Rightarrow u \cos \theta = v \sin \theta$$

$$\Rightarrow \frac{u}{v} = \frac{\sin \theta}{\cos \theta}$$

$$\Rightarrow \tan \theta = \frac{u}{v}$$

BY RESTITUTION, PERPENDICULAR TO THE WALL

$$\Rightarrow e = \frac{\text{SEP}}{\text{APP}}$$

$$\Rightarrow e = \frac{v \cos \theta}{u \sin \theta}$$

$$\Rightarrow \frac{1}{e} = \frac{u \sin \theta}{v \cos \theta}$$

$$\Rightarrow \frac{1}{e} = \frac{u}{v} \tan \theta$$

COMBINING EQUATIONS FROM ABOVE

$$\frac{1}{e} = \tan^2 \theta$$

$$\tan \theta = +\sqrt{\frac{1}{e}} \quad (\theta \text{ acute})$$

$$\tan \theta = \frac{1}{\sqrt{e}}$$

AS REQUIRED

b) FINALLY WE HAVE

$$0 < e < 1$$

$$0 < \sqrt{e} < 1$$

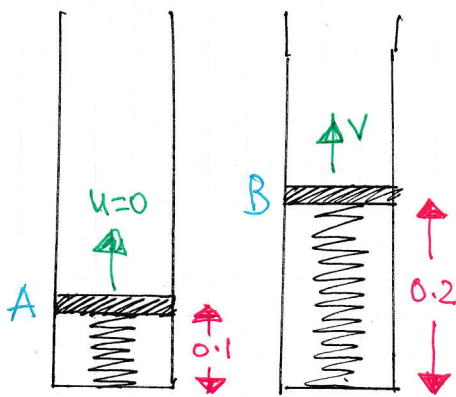
$$1 < \frac{1}{\sqrt{e}} < \infty$$

$$\therefore \tan \theta > 1$$

$$\therefore \underline{45 < \theta < 90}$$

-1-

1YGB - Full Paper 0 - Question 2



$$\begin{aligned} \lambda &= 2000 \text{ N} \\ l &= 0.2 \text{ m} \\ m &= 1.5 \text{ kg} \end{aligned}$$

BY ANSWERING TAKING THE LEVEL OF "A"
AS THE ZERO GRAVITATIONAL POTENTIAL
LEVEL

$$\Rightarrow \cancel{KE_A} + \cancel{PE_A} + \cancel{EE_A} + \cancel{W_{in}} - \cancel{W_{out}} = \cancel{KE_B} + \cancel{PE_B} + \cancel{EE_B}$$

$$\Rightarrow \frac{\lambda}{2l} x^2 - F \times d = \frac{1}{2} m v^2 + mgh$$

$$\Rightarrow \frac{2000}{2(0.2)} (0.1)^2 - (5.3)(0.1) = \frac{1}{2} (1.5) v^2 + (1.5)(9.8)(0.1)$$

$$\Rightarrow 50 - 0.53 = 0.75 v^2 + 1.47$$

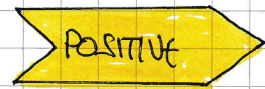
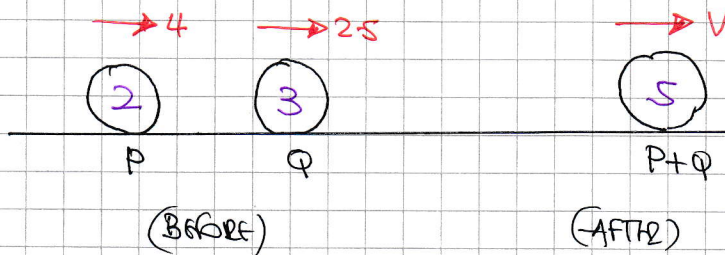
$$\Rightarrow 48 = 0.75 v^2$$

$$\Rightarrow v^2 = 64$$

$$\Rightarrow |v| = 8 \text{ ms}^{-1}$$

1YGB - FMI PAPER 0 - QUESTION 3

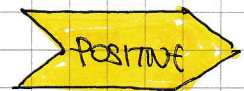
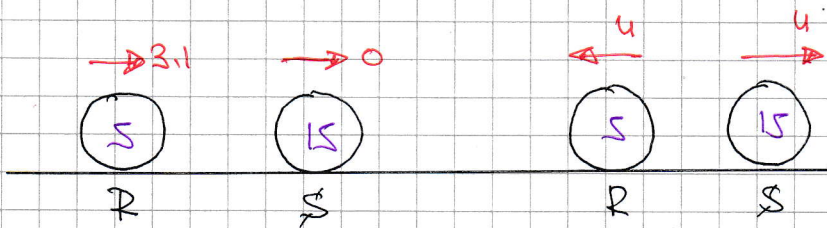
a) START WITH A COLLISION DIAGRAM



BY CONSERVATION OF MOMENTUM

$$(2 \times 4) + (3 \times 2.5) = 5V$$
$$8 + 7.5 = 5V$$
$$5V = 15.5$$
$$V = 3.1 \text{ ms}^{-1}$$

b) BEGINNING A NEW DIAGRAM



BY MOMENTUM CONSERVATION

$$(5 \times 3.1) + 0 = -5u + 15u$$
$$15.5 = 10u$$
$$u = 1.55 \text{ ms}^{-1}$$

FINALLY AS THE PARTICLES MOVE IN OPPOSITE DIRECTION, WITH EQUAL SPEEDS OF 1.55 ms^{-1}

EVERY SECOND THEY MOVE $(1.55 + 1.55)$ METRES APART

$$\therefore d = 3.6 \times 2 \times 1.55$$
$$d = 11.16 \text{ m}$$

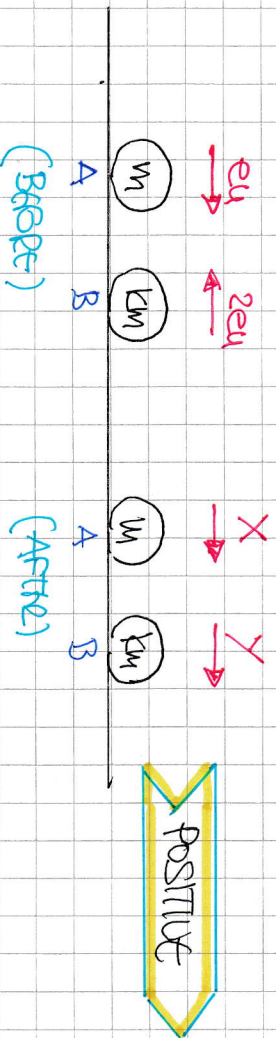
1X6-B - FM1 PAPER 0 - QUESTION 4

STARTING WITH THE COLLISIONS WITH THE WALLS

AFTER REBOUNDING

$$V_A = eu \quad \& \quad V_B = 2eu$$

NEXT THE COLLISION BETWEEN THEM



BY CONSERVATION OF MOMENTUM

$$\Rightarrow me u - 2kme u = mX + kmY$$

$$\Rightarrow eu - 2keu = X + kY$$

BY THE RESTITUTION COEFFICIENT

$$\Rightarrow \frac{Y - X}{eu + 2eu} = e$$

$$\Rightarrow -X + Y = 3eu^2$$

$$\Rightarrow \boxed{kX - kY = -3keu^2} \quad \times (-k)$$

ADDING THE EQUATIONS

$$kX - kY = -3keu^2$$

$$X + kY = eu - 2keu$$

$$(k+1)X = eu - 2keu - 3keu^2$$

$$X = \frac{eu(1 - 2k - 3ke)}{(k+1)}$$

A DOES NOT REVERSE ITS DIRECTION

$$X > 0$$

$$\Rightarrow \frac{eu(1 - 2k - 3ke)}{k+1} > 0$$

$$\Rightarrow 1 - 2k - 3ke > 0 \quad [eu > 0, k+1 > 0]$$

$$\Rightarrow -3ke > 2k - 1$$

$$\Rightarrow e < \frac{1 - 2k}{3k}$$

As required

— 1 —

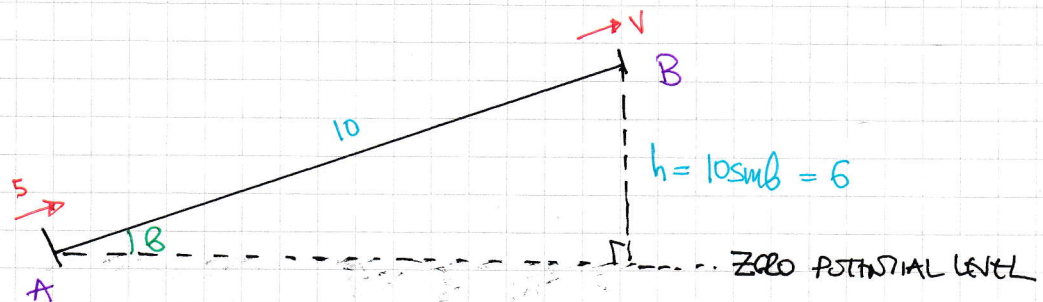
LYGB - FMI PAPER P - QUESTION 5

AUXILIARIES FIRST

$$\tan b = \frac{3}{4} \Rightarrow \begin{array}{c} 3 \\ \diagup \\ 5 \\ \diagdown \\ 4 \end{array} \Rightarrow \begin{array}{l} \sin b = \frac{3}{5} \\ \cos b = \frac{4}{5} \end{array}$$

ONLY THE COMPONENT OF THE TENSION PARALLEL TO THE PLANT PUTS ENERGY INTO THE SYSTEM, I.E. $1500 \cos b = 1500 \times \frac{4}{5} = 1200$

NOW LOOKING AT AN ENERGY DIAGRAM, AND TAKING THE LEVEL OF "A" AS THE ZERO GRAVITATIONAL POTENTIAL LEVEL



$$\Rightarrow K.E._A + \cancel{P.E._A} + W_{in} - W_{out} = K.E._B + P.E._B$$

$$\Rightarrow \frac{1}{2}(120) \times 5^2 + 0 + (1200 \times 10) - (180 \times 10) = \frac{1}{2}(120)v^2 + 120g \times 6 \leftarrow \text{"mgh"}$$

$$\Rightarrow 1500 + 1200 - 1800 = 60v^2 + 7056$$

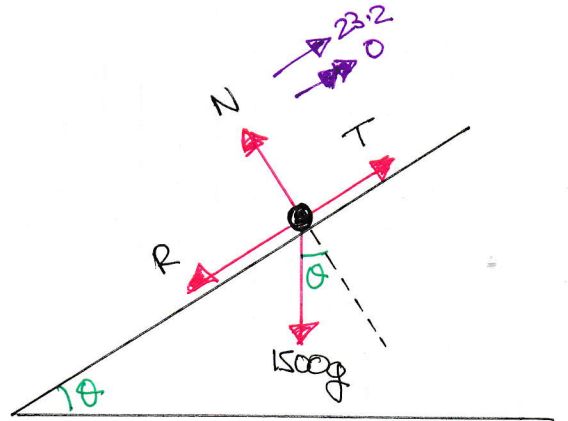
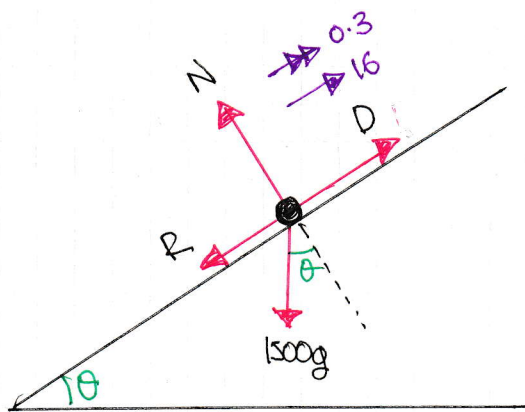
$$\Rightarrow 4644 = 60v^2$$

$$\Rightarrow v^2 = 77.4$$

$$\Rightarrow |v| \approx 8.80 \text{ ms}^{-1}$$

IYGB - FMI PAPER 0 - QUESTION 6

- ① START WITH TWO SEPARATE DIAGRAMS, TRYING TO GET EQUATIONS



② "P = Dv"

$$\Rightarrow P = D \times 16$$

$$\Rightarrow D = \frac{P}{16}$$

- ③ EQUATION OF MOTION

$$\Rightarrow "F = ma"$$

$$\Rightarrow D - R - 1500g \sin\theta = 1500a$$

$$\Rightarrow \frac{P}{16} - R - 1500g\left(\frac{2}{49}\right) = 1500(0.3)$$

$$\Rightarrow \frac{P}{16} - R - 600 = 450$$

$$\Rightarrow \underline{\frac{P}{16} - R = 1050}$$

④ "P = Tv"

$$\Rightarrow P = T \times 23.2$$

$$\Rightarrow T = \frac{P}{23.2}$$

- ⑤ NO ACCELERATION (EQUILIBRIUM)

$$\Rightarrow T = R + 1500g \sin\theta$$

$$\Rightarrow \frac{P}{23.2} = R + 1500(9.8)\left(\frac{2}{49}\right)$$

$$\Rightarrow \frac{P}{23.2} = R + 600$$

$$\Rightarrow \underline{\frac{P}{23.2} - R = 600}$$

- ⑥ COMBINING EQUATIONS BY SUBTRACTION

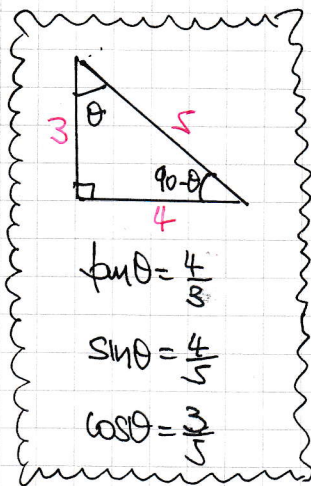
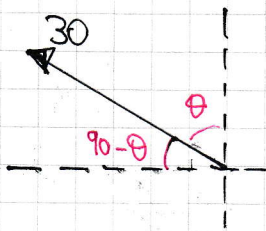
$$\frac{P}{16} - \frac{P}{23.2} = 450 \Rightarrow 23.2P - 16P = 167040$$

$$\Rightarrow 7.2P = 167040$$

$$P = 23200$$

1YGB - FMI PAPER 2 - QUESTION 7

STARTING WITH A DIAGRAM



IMPULSE = MOUNTAIN AFTER - MOUNTAIN BEFORE

$$\underline{I} = m\underline{v} - m\underline{u}$$

$$(-30 \sin \theta) \underline{i} + (30 \cos \theta) \underline{j} = 0.5 \underline{v} - 0.5 \times 40 \underline{i}$$

$$-30(0.8) \underline{i} + 30(0.6) \underline{j} = 0.5 \underline{v} - 20 \underline{i}$$

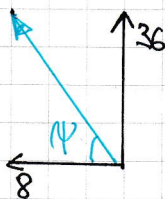
$$-24 \underline{i} + 18 \underline{j} = 0.5 \underline{v} - 20 \underline{i}$$

$$-4 \underline{i} + 18 \underline{j} = 0.5 \underline{v}$$

$$\underline{v} = -8 \underline{i} + 36 \underline{j}$$

$$\therefore |\underline{v}| = \sqrt{(-8)^2 + 36^2} = \sqrt{1360} \approx \underline{36.9 \text{ ms}^{-1}}$$

FIND THE REQUIRED ANGLE



$$\tan \psi = \frac{36}{8} = \frac{9}{2}$$

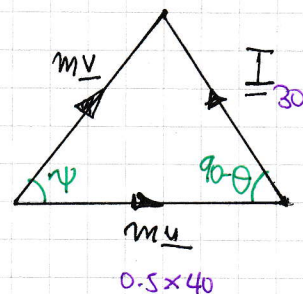
$$\underline{\psi \approx 77.5^\circ}$$

ALTERNATIVE BY GEOMETRY

$$\underline{I} = m\underline{v} - m\underline{u}$$

$$m\underline{u} + \underline{I} = m\underline{v}$$

DRAWING A VECTOR TRIANGLE



YGB - FMI PAPER P - QUESTION 7

BY THE COSINE RULE

$$|m\mathbf{v}|^2 = |m\mathbf{u}|^2 + |\mathbf{I}|^2 - 2|m\mathbf{u}||\mathbf{I}|\cos(90-\theta)$$

$$|0.5\mathbf{v}|^2 = 20^2 + 30^2 - 2 \times 20 \times 30 \times \sin\theta$$

$$\cos(90-\theta) = \sin\theta$$

$$\frac{1}{4}|\mathbf{v}|^2 = 400 + 900 - 1200 \times \frac{4}{5} \leftarrow (\text{FROM BEFORE})$$

$$\frac{1}{4}|\mathbf{v}|^2 = 340$$

$$|\mathbf{v}|^2 = 1360$$

$$|\mathbf{v}| = \sqrt{1360} \approx 36.9 \text{ m/s}$$

As before

AND BY THE SINE RULE

$$\frac{\sin\psi}{|\mathbf{I}|} = \frac{\sin(90-\theta)}{|m\mathbf{v}|} \Rightarrow \frac{\sin\psi}{30} = \frac{\cos\theta}{\frac{1}{2}\sqrt{1360}}$$

$$\Rightarrow \frac{\sin\psi}{30} = \frac{0.6}{\frac{1}{2}\sqrt{1360}}$$

$$\Rightarrow \sin\psi = 0.976187 \dots$$

$$\Rightarrow \psi \approx 77.5^\circ$$

As before

IYGB - FMI PAPER P - QUESTION 8

BY HOOKE'S LAW - LET THE NATURAL LENGTH BE l

$$mg = \frac{\lambda}{l}(x-l)$$

$$mgl = \lambda(x-l)$$

$$\frac{mgl}{\lambda} = x-l$$

$$\frac{gl}{\lambda} = \frac{x-l}{m}$$

$$\text{a } Mg = \frac{\lambda}{l}(y-l)$$

$$Mgl = \lambda(y-l)$$

$$\frac{Mgl}{\lambda} = y-l$$

$$\frac{gl}{\lambda} = \frac{y-l}{M}$$

EQUATING YIELDS

$$\Rightarrow \frac{x-l}{m} = \frac{y-l}{M}$$

$$\Rightarrow Mx - Ml = my - ml$$

$$\Rightarrow Mx - my = Ml - ml$$

$$\Rightarrow Mx - my = l(M-m)$$

$$\Rightarrow l = \frac{Mx - my}{M - m}$$

As $l > 0$ & $M > m$, so THAT $M - m > 0$, IT IMPLIES THAT

$$\Rightarrow Mx - my > 0$$

$$\Rightarrow \underline{Mx > my}$$

AS REQUIRED