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Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

A-level MATHEMATICS

Paper 1

Tuesday 4 June 2024

Afternoon

Time allowed: 2 hours

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
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TOTAL	



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Answer **all** questions in the spaces provided.

- 1** Find the coefficient of x in the expansion of

$$(4x^3 - 5x^2 + 3x - 2)(x^5 + 4x + 1)$$

Circle your answer.

[1 mark]

-5

-2

7

11



2 The function f is defined by $f(x) = e^x + 1$ for $x \in \mathbb{R}$

Find an expression for $f^{-1}(x)$

Tick (✓) **one** box.

[1 mark]

$f^{-1}(x) = \ln(x - 1)$

$f^{-1}(x) = \ln(x) - 1$

$f^{-1}(x) = \frac{1}{e^x + 1}$

$f^{-1}(x) = \frac{x - 1}{e}$

Turn over for the next question

Turn over ►



3 The expression

$$\frac{12x^2 + 3x + 7}{3x - 5}$$

can be written as

$$Ax + B + \frac{C}{3x - 5}$$

State the value of A

Circle your answer.

[1 mark]

3

4

7

9

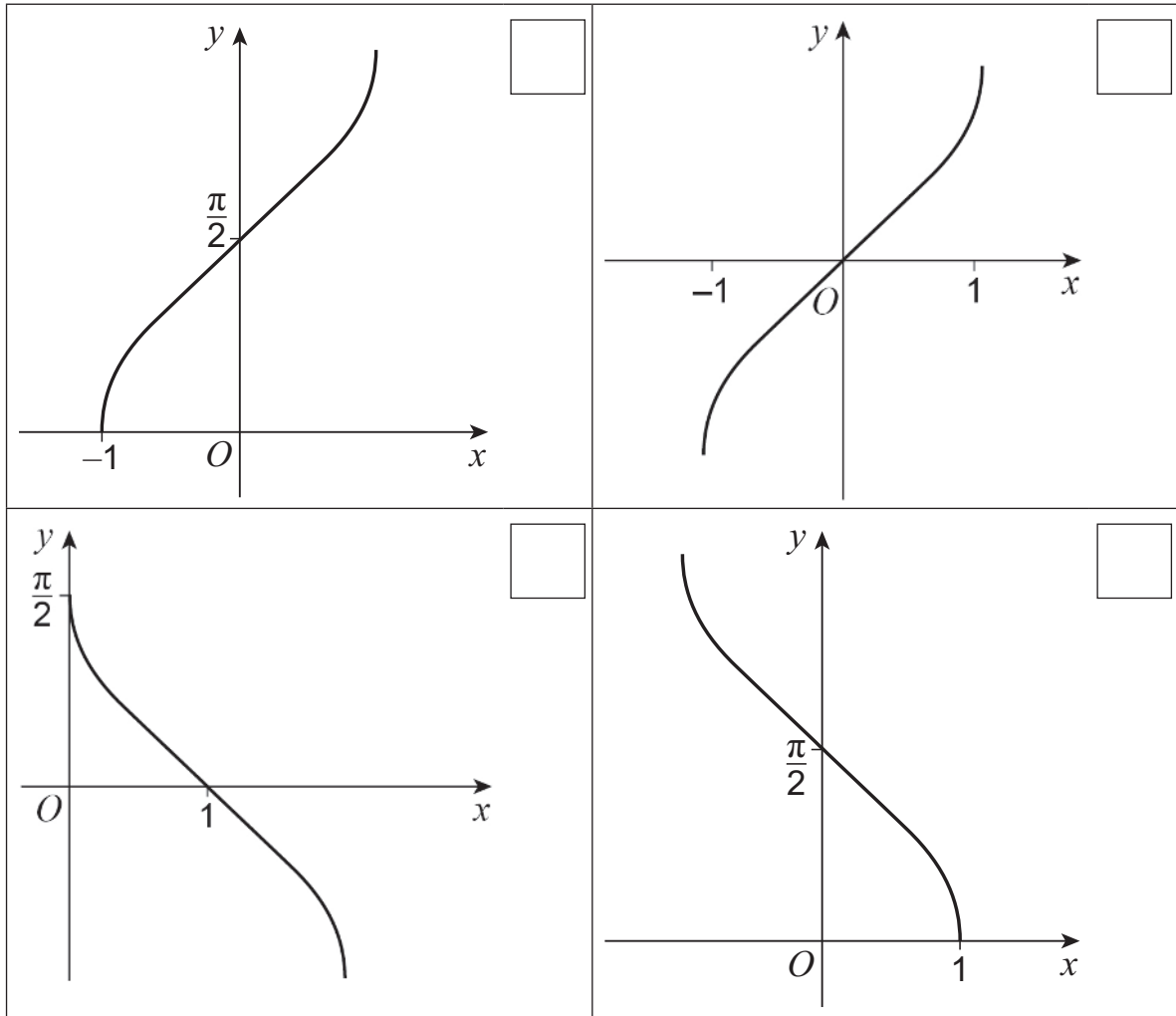


4 One of the diagrams below shows the graph of $y = \arccos x$

Identify the graph of $y = \arccos x$

Tick (✓) **one** box.

[1 mark]



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- 8 (a)** Find the first three terms, in ascending powers of x , in the expansion of

$$(2 + kx)^5$$

where k is a positive constant.

[3 marks]

- 8 (b)** Hence, given that the coefficient of x is four times the coefficient of x^2 , find the value of k

[2 marks]

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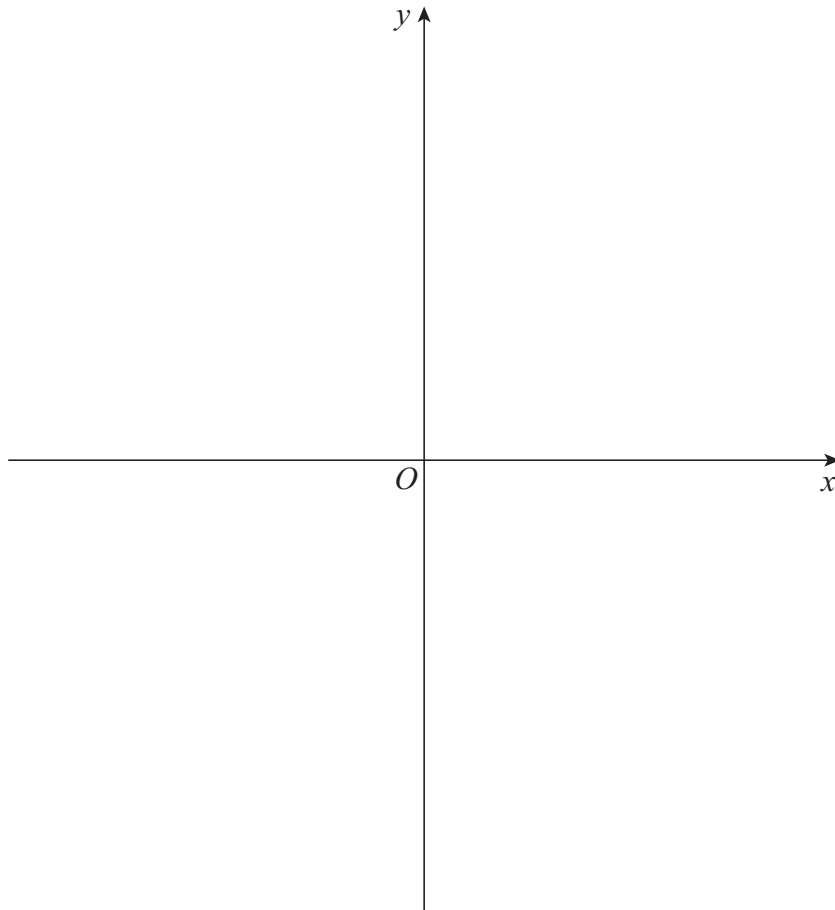
11 It is given that

$$f(x) = x(x - a)(x - 6)$$

where $0 < a < 6$

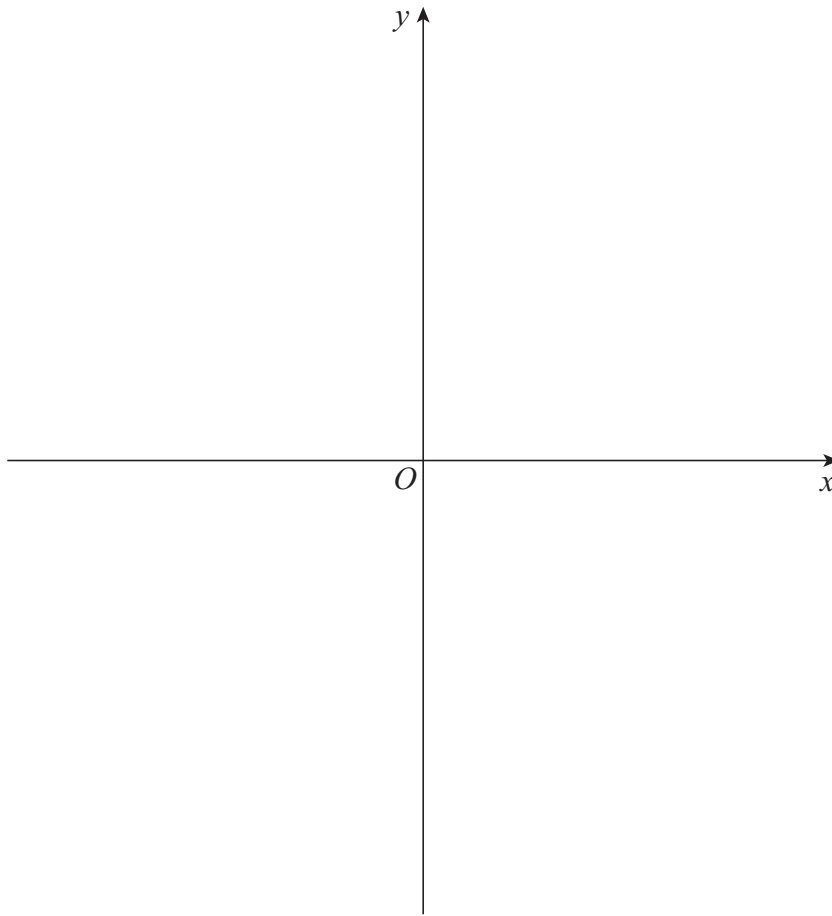
11 (a) Sketch the graph of $y = f(x)$ on the axes below.

[3 marks]



11 (b) Sketch the graph of $y = f(-2x)$ on the axes below.

[2 marks]



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13 (a) It is given that

$$P(x) = 4x^3 + 8x^2 + 11x + 4$$

Use the factor theorem to show that $(2x + 1)$ is a factor of $P(x)$

[2 marks]

13 (b) Express $P(x)$ in the form

$$P(x) = (2x + 1)(ax^2 + bx + c)$$

where a , b and c are constants to be found.

[2 marks]



- 13 (c)** Given that n is a positive integer, use your answer to part (b) to explain why $4n^3 + 8n^2 + 11n + 4$ is **never** prime.

[2 marks]

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14 (c) (ii) **Figure 1** below shows a sketch of parts of the graphs of

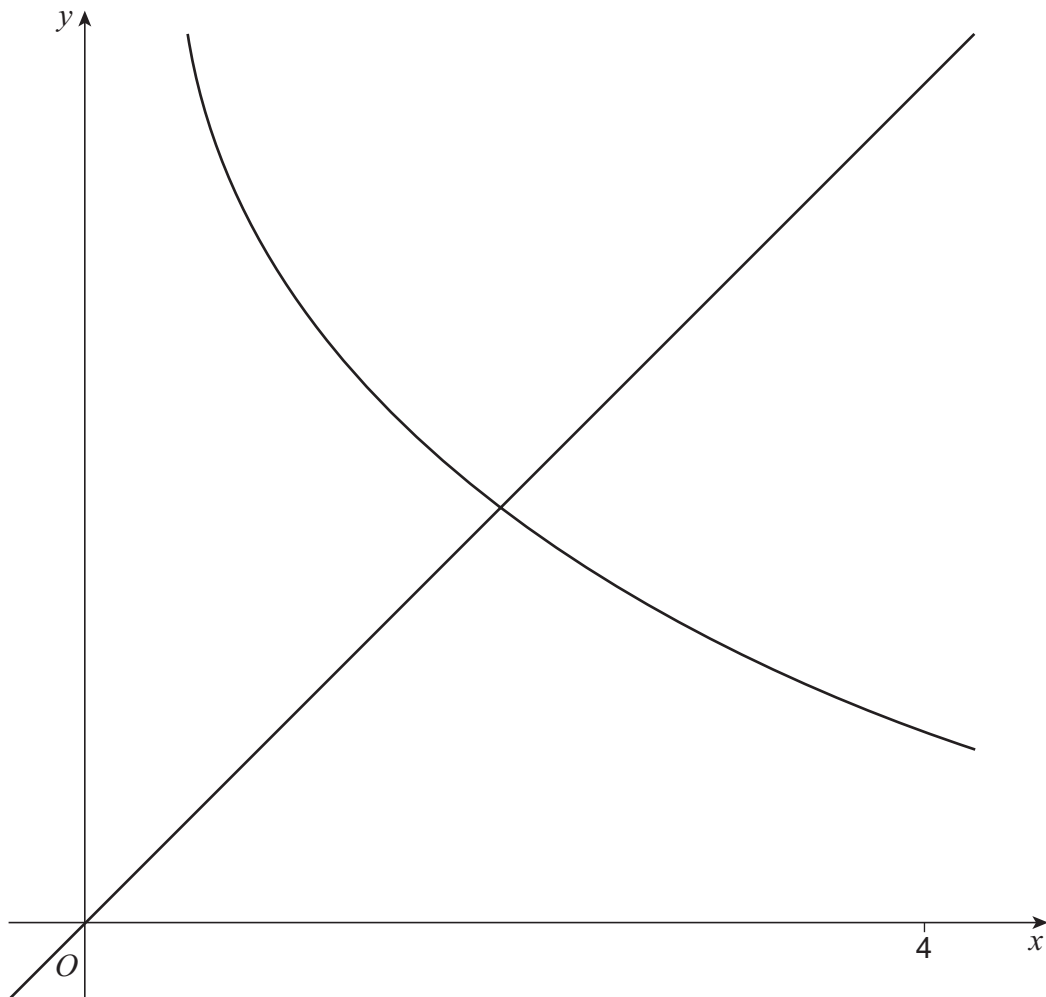
$$y = 3 - \frac{3}{2} \ln x \text{ and } y = x$$

On **Figure 1**, draw a staircase or cobweb diagram to show how convergence takes place.

Label, on the x -axis, the positions of x_2 , x_3 and x_4

[2 marks]

Figure 1



14 (c) (iii) Explain why the iterative formula

$$x_{n+1} = 3 - \frac{3}{2} \ln x_n$$

fails to converge to α when the starting value is $x_1 = 0$

[1 mark]

Turn over for the next question

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15 (b) A student is attempting to solve the equation

$$\sin 2\theta \operatorname{cosec} \theta + \cos 2\theta \sec \theta = 3 \text{ for } 0^\circ \leq \theta \leq 360^\circ$$

They use the result from part (a), and write the following **incorrect** solution:

$$\sin 2\theta \operatorname{cosec} \theta + \cos 2\theta \sec \theta = 3$$

Step 1 $4 \cos \theta - \sec \theta = 3$

Step 2 $4 \cos \theta - \frac{1}{\cos \theta} - 3 = 0$

Step 3 $4 \cos^2 \theta - 3 \cos \theta - 1 = 0$

Step 4 $\cos \theta = 1$ or $\cos \theta = -0.25$

Step 5 $\theta = 0^\circ, 104.5^\circ, 255.5^\circ, 360^\circ$

15 (b) (i) Explain why the student should reject one of their values for $\cos \theta$ in Step 4.

[1 mark]

15 (b) (ii) State the correct solutions to the equation

$$\sin 2\theta \operatorname{cosec} \theta + \cos 2\theta \sec \theta = 3 \text{ for } 0^\circ \leq \theta \leq 360^\circ$$

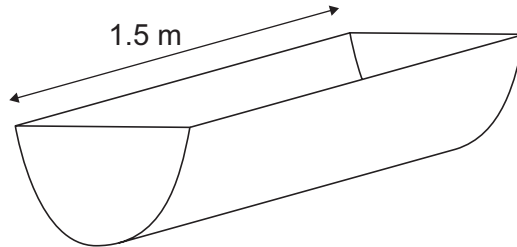
[1 mark]

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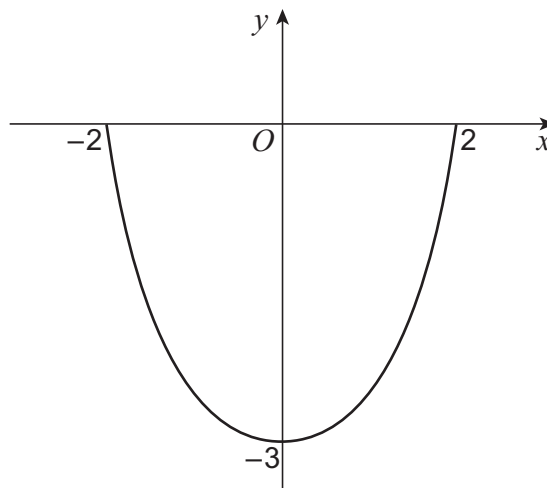
- 16 **Figure 2** below shows a 1.5 metre length of pipe.

Figure 2



The symmetrical cross-section of the pipe is shown below, in **Figure 3**, where x and y are measured in centimetres.

Figure 3



17 The function f is defined by

$$f(x) = |x| + 1 \text{ for } x \in \mathbb{R}$$

The function g is defined by

$$g(x) = \ln x$$

where g has its greatest possible domain.

17 (a) Using set notation, state the range of f

[2 marks]

17 (b) State the domain of g

[1 mark]

17 (c) The composite function h is given by

$$h(x) = gf(x) \text{ for } x \in \mathbb{R}$$

17 (c) (i) Write down an expression for $h(x)$ in terms of x

[1 mark]



17 (c) (ii) Determine if h has an inverse.

Fully justify your answer.

[2 marks]

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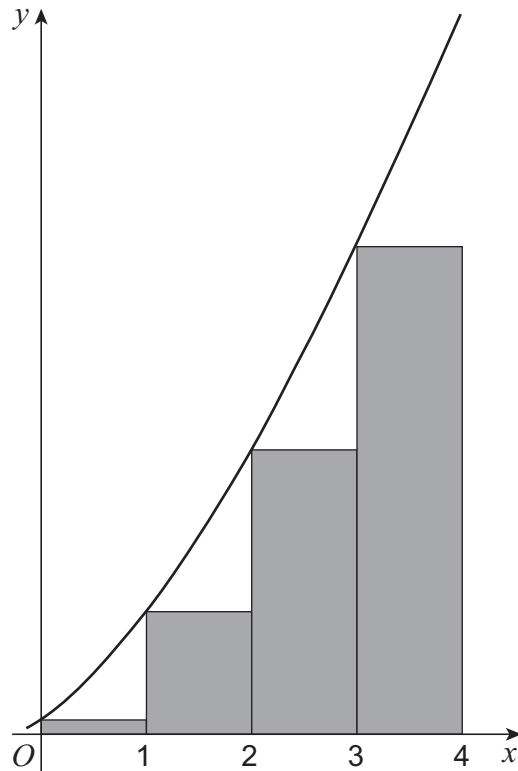
18 (c) A graph has the equation

$$y = (4x + 1)\sqrt{2x + 1}$$

A student uses four rectangles to approximate the area under the graph between the lines $x = 0$ and $x = 4$

The rectangles are all the same width.

All the rectangles are drawn under the curve as shown in the diagram below.



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